



Particle Transport, Deposition and Removal 

Particle Removal From Rough Surfaces

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Outline



- **van der Waals/Pull-off Force for Rough Surfaces**
- **Rolling and Sliding Removal of Rough Particles**
- **Hydrodynamic Forces and Torque**
- **Critical Shear Velocity for Detachment**

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JKR Adhesion Model



Pull-Off Force $\Rightarrow F_{po}^{JKR} = \frac{3}{4} \pi W_A d$

Contact Radius at Separation


$a = \left(\frac{3\pi W_A d^2}{8K} \right)^{1/3}$

$a = \left(\frac{F_{Po} d}{2K} \right)^{1/3}$

$K = \frac{4}{3} \left[\frac{(1-\nu_1^2)}{E_1} + \frac{(1-\nu_2^2)}{E_2} \right]^{-1}$

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Rough Surfaces



Pull-Off Force $\Rightarrow F_M = \pi a^2 N f_{Po} e^{-0.6/\Delta_c}$

$\Delta_c = \frac{\delta_c}{\sigma}$

- Max Asperity Extension
- Roughness Height Standard deviation
- Number of Pull-Off Force Asperities per Unit Area for each Asperity

Contact Radius $\xrightarrow{\text{Estimated}}$ $a = \left(\frac{F_M d}{2K} \right)^{1/3}$

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Rough Surfaces Clarkson University

JKR Model

$$\delta_c = \left[\frac{f_{Po}^2}{3K^2\beta} \right]^{1/3}$$

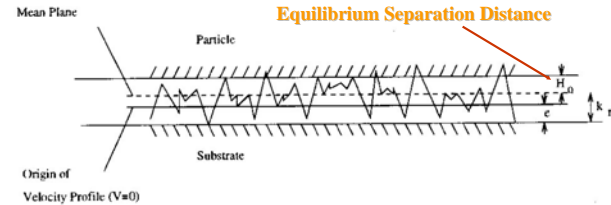
Greenwood-Williamson

$$\sigma\beta N \approx 0.1$$

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Contact of Rough Surfaces Clarkson University



Average Roughness Height

$$k_r = 5.9\sigma$$

Displaced Origin of Velocity Profile

$$e = 0.53k_r$$

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Hydrodynamic Forces Clarkson University

Drag Force

$$F_t = \frac{3\pi\mu d}{C_c} V$$

Lift Force

$$F_l = 1.61d^2V(\rho\mu)^{1/2} \frac{dV/dy}{|dV/dy|^{1/2}}$$

Hydrodynamic Torque

$$M_t = \frac{2\pi\mu f_m d^2 V}{C_c}$$

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Sublayer Model Clarkson University

$$u^+ = y^+$$

$$v^+ = -\beta_o y^{+2}, y^+ \leq 1.85$$

$$w^+ = 2\beta_o y^+ z^+$$

$$\beta_o = 0.01085$$

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Velocity at Particle Centroid Clarkson University

$$u^+ = \frac{d^+}{2} + 2.76\sigma^+ + H_0^+ - \alpha^+ = L^+$$

$$w^+ = \beta \frac{\Lambda^+}{2} \left(\frac{d^+}{2} + 2.76\sigma^+ + H_0^+ - \alpha^+ \right)$$

$$L = \frac{d}{2} + 2.76\sigma + H_0 - \alpha$$

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Hydrodynamic Forces Clarkson University

Drag Force $\Rightarrow F_t = \frac{5.8\pi\rho d u^*{}^2 L}{C}$

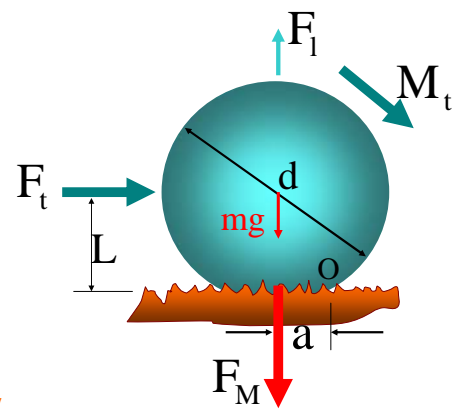
Lift Force $\Rightarrow F_L = \frac{1.95\rho d^2 u^*{}^3 L}{\nu}$

Hydrodynamic Torque $\Rightarrow M_t = \frac{2.14\pi\rho u^*{}^2 d^2 L}{C}$

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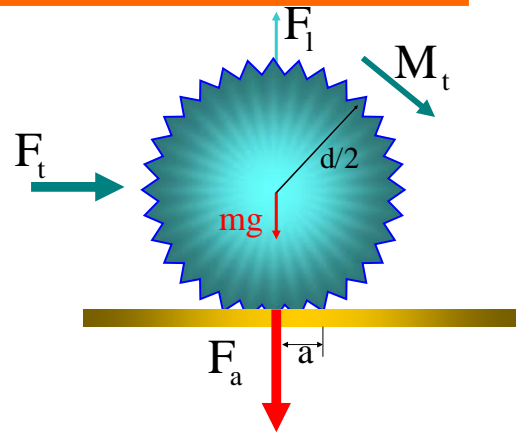
Particle-Surface Contact Clarkson University



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Rough Particle Clarkson University



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Detachment Model Clarkson University

MOMENT DETACHMENT

$$M_t + F_t \left(\frac{d}{2} - \alpha_0 \right) + (F_L - mg)a \geq F_M a$$

SLIDING DETACHMENT

$$F_t \geq k(F_M + mg - F_L)$$

Detachment Models- Sublayer Clarkson University

Rolling

$$u_c^* = \left[\frac{aC[\pi a^2 N f_{po} \exp[-0.6/(\Delta_c)^2] + mg]}{\rho L d^2 (5.04\pi + 1.95 \frac{aC u_c^*}{v})} \right]^{1/2}$$

Sliding

$$u_c^* = \left[\frac{kC[\pi a^2 N f_{po} \exp[-0.6/(D_c)^2] + mg]}{\rho L d (5.8\pi + 1.95 \frac{kC d u_c^*}{v})} \right]^{1/2}$$

Detachment Models-Burst Clarkson University

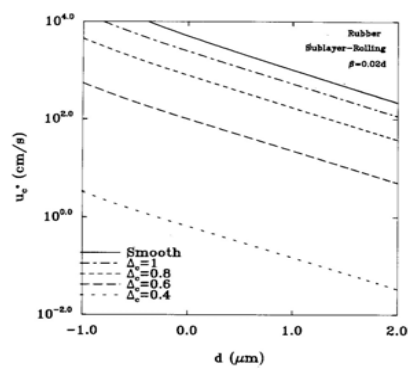
Rolling

$$u_c^* = \left[\frac{aC(\pi a^2 N f_{po} \exp[-0.6/(\Delta_c)^2] + mg)}{\rho L d^2 (1.72 + 0.1 \frac{u_c^* L}{v}) \left(5.04\pi + 1.95 \frac{aC u_c^*}{v} (1.72 + 0.2 \frac{u_c^* L}{v})^{1/2} \right)} \right]^{1/2}$$

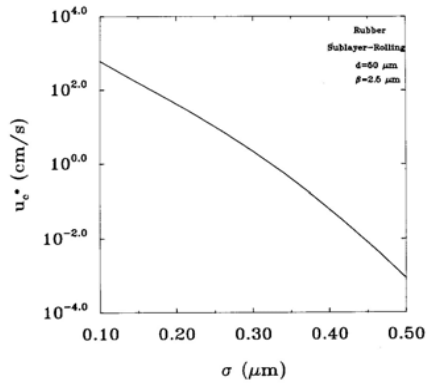
Sliding

$$u_c^* = \left[\frac{kC[\pi a^2 N f_{po} \exp[-0.6/(\Delta_c)^2] + mg]}{\rho d L (1.72 + 0.1 \frac{u_c^* L}{v}) \left(5.8\pi + 1.95 \frac{kC d u_c^*}{v} (1.72 + 0.2 \frac{u_c^* L}{v})^{1/2} \right)} \right]^{1/2}$$

Critical Detachment Shear Velocity Clarkson University



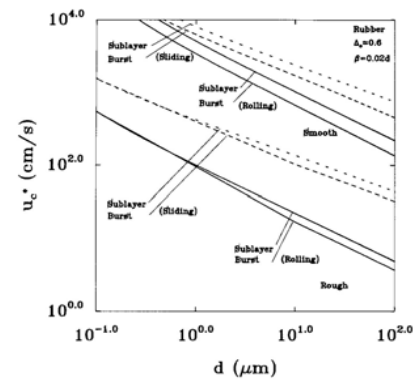
Critical Detachment Shear Velocity



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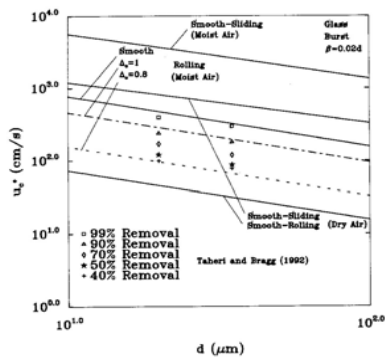
Critical Detachment Shear Velocity



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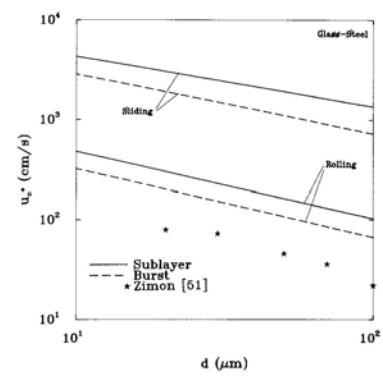
Critical Detachment Shear Velocity



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Comparison with Zimon

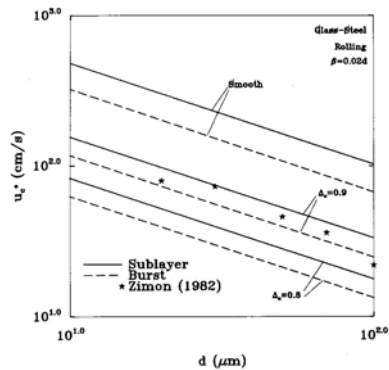


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Critical Detachment Shear Velocity

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Conclusions

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- Rolling detachment is the dominant mechanism for detachment of rough spherical particles.
- Roughness significantly reduces the adhesion pull-off force.
- Turbulence near wall flow structure plays an important role in particle detachment process.
- Accounting for surface roughness improves the agreement between the model prediction and experimental data

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Thank you!

Questions?

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