

Name: _____

(1 Hour)

Problem 1: A 4 kg/s steady flow of ammonia runs through a device where it goes through a Polytropic process. The inlet state is 150 kPa, -20°C and the exit state is 400 kPa, 80°C , where all kinetic and potential energies can be neglected. The specific work input has been found to be given as $[\mathbf{n}/(\mathbf{n}-1)] \Delta(\mathbf{Pv})$.

a) Find the Polytropic exponent \mathbf{n}

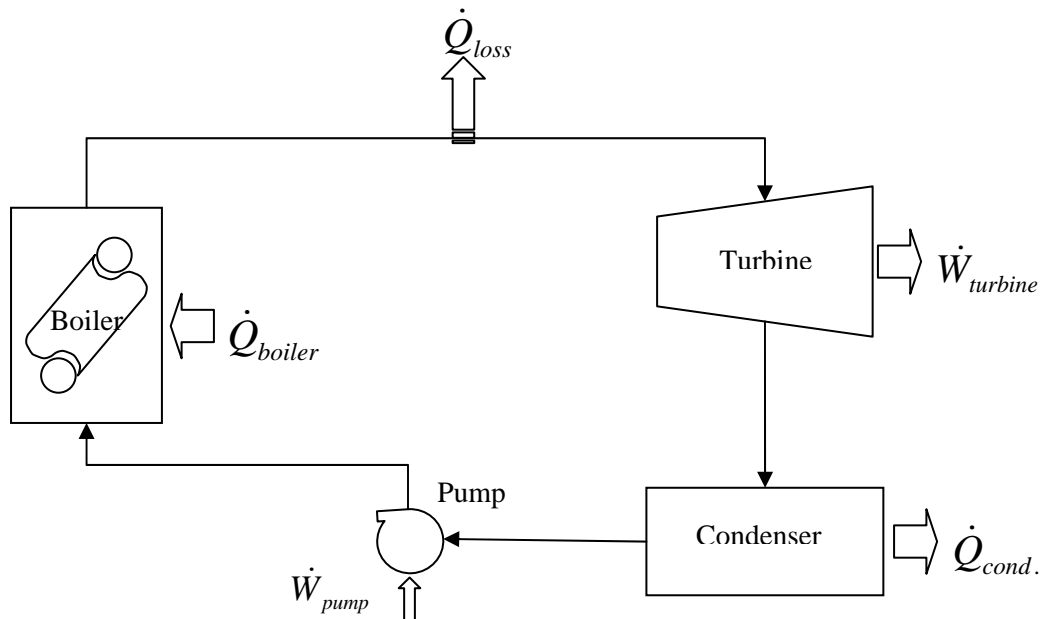
b) Find the specific work and the specific heat transfer.

(5 points)

Hints:

1. Polytropic process: $\mathbf{Pv}^{\mathbf{n}} = \text{constant}$ 2. $\ln(x^y) = y \ln(x)$, $\ln\left(\frac{x}{y}\right) = \ln(x) - \ln(y)$

Problem 2: Consider a simple steam power plant, as shown in Figure 1. The following data are for such a power plant.



Location	Pressure	Temperature/Quality
Leaving boiler	2.0 MPa	300°C
Entering turbine	1.9 MPa	290°C
Leaving turbine, entering condenser	15 KPa	90%
Leaving condenser, entering pump	14 KPa	45°C

For pump work = 4 KJ/Kg and negligible potential and kinetic energies, determine the following quantities per kilogram flowing through the unit:

- Show the states at each connection in a T-v diagram and explain your assumptions.
- Heat Transfer in line between boiler and turbine.
- Turbine work.
- Heat transfer in condenser.
- Heat transfer in boiler.

(10 points)

Hints: Use control volume balances of mass and energy for each device in the unit

PROBLEM 1.

Ammonia, steady state

polytropic

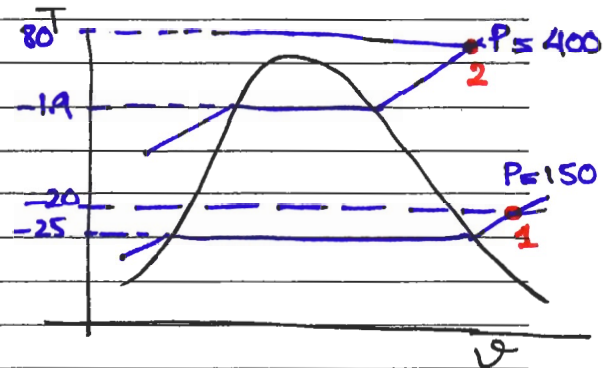
$$\Delta PE = \Delta KE = 0$$

$$\textcircled{1} \quad P_1 = 150 \text{ Kpa} \xrightarrow[\text{A14}]{\text{Table}} T_{\text{sat}1} = -25^\circ\text{C}$$

$$T_1 = -20^\circ\text{C}$$

$$\textcircled{2} \quad P_2 = 400 \text{ Kpa} \xrightarrow[\text{A14}]{\text{Table}} T_{\text{sat}2} = -1.9^\circ\text{C}$$

$$T_2 = 80^\circ\text{C}$$



So both states $\textcircled{1}$ & $\textcircled{2}$ are superheated vapors.

Using table A15, $\left\{ \begin{array}{l} \textcircled{1}: v_1 = 0.7978 \text{ m}^3/\text{kg}, h_1 = 1422.67 \text{ kJ/kg} \\ \textcircled{2}: v_2 = 0.4216, h_2 = 1636.41 \text{ kJ/kg} \end{array} \right.$

Mass Balance:

$$\underbrace{\frac{dm_{\text{cv}}}{dt}}_{\text{s.s.}} = \sum \dot{m}_i - \sum \dot{m}_e \rightarrow \boxed{m_1 = m_2 = \dot{m}} \quad (\text{I})$$

Energy Balance:

$$\underbrace{\frac{dE_{\text{cv}}}{dt}}_{\text{s.s.}} = \sum \dot{Q}_{\text{cv}} - \sum \dot{W}_{\text{cv}} + \sum \dot{m}_i \left(h_i + \frac{V_i^2}{2} + g z_i \right) - \sum \dot{m}_e \left(h_e + \frac{V_e^2}{2} + g z_e \right)$$

(Prob. St.)
(Prob. St.)

using (I): $0 = \dot{Q} - \dot{W} + \dot{m}(h_1 - h_2) \xrightarrow{\text{divide by } \dot{m}} \boxed{q = w + h_2 - h_1}$

Polytropic process:

$$P v^n = \text{constant} \quad \text{or} \quad P_1 v_1^n = P_2 v_2^n \rightarrow \frac{P_1}{P_2} = \left(\frac{v_2}{v_1} \right)^n$$

taking Natural log; $\ln \left(\frac{P_1}{P_2} \right) = n \ln \left(\frac{v_2}{v_1} \right)$

Prob. 1 (cont'd)

plugging for P_1, P_2, v_1, v_2 gives:

$$n = \frac{\ln\left(\frac{P_1}{P_2}\right)}{\ln\left(\frac{v_1}{v_2}\right)} = \frac{\ln\left(\frac{150}{400}\right)}{\ln\left(\frac{0.4216}{0.7978}\right)} = \underline{\underline{1.538}} \quad \text{Ans. (a)}$$

$$w = \frac{n}{n-1} \Delta(Pv^n) = \frac{n}{n-1} (P_2 v_2^n - P_1 v_1^n)$$
$$= \frac{1.538}{1.538-1} (-150 \times 0.7978 + 400 \times 0.4216)$$

$$\rightarrow w = 140.02 \text{ KJ/kg} \quad \text{Ans. (b)}$$

$$\rightarrow w_{\text{input}} = \underline{\underline{-140.02}} \text{ KJ/kg}, \quad \dot{w}_{\text{input}} = \underline{\underline{-560.08}} \text{ Kg}$$

$$q = w + h_2 - h_1 = -140.02 + (1636.41 - 1422.67)$$

$$\rightarrow \dot{q} = \underline{\underline{73.72}} \text{ KJ/kg}, \quad \dot{Q} = \underline{\underline{294.88}} \text{ Kg}$$

point:

$$W = \int p dv \quad \text{or} \quad \int v dp$$

① ②

$$\left\{ \begin{array}{l} \text{if you use ①} \rightarrow W = \frac{\Delta(Pv^n)}{1-n} \quad \text{Work done by} \\ \text{Comp/Exp.} \end{array} \right.$$

$$\left\{ \begin{array}{l} \text{" " " ②} \rightarrow W = \frac{n}{n-1} \Delta(Pv^n) \quad \text{Work done by} \\ \text{a pump} \end{array} \right.$$

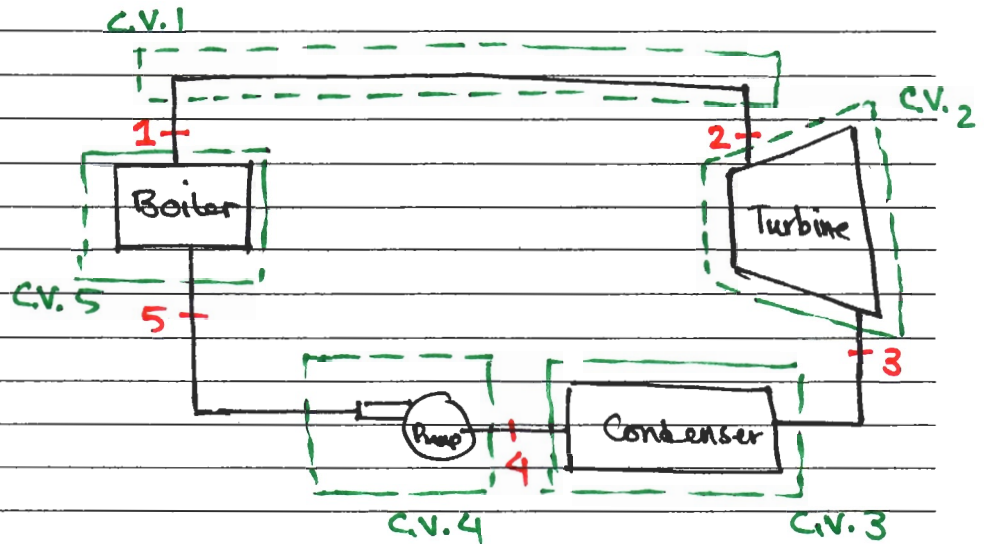
PROBLEM 2.

Steam

Steady state

$$\Delta PE = 0, \Delta KE = 0$$

$$\dot{Q}_T = \dot{Q}_P = 0$$

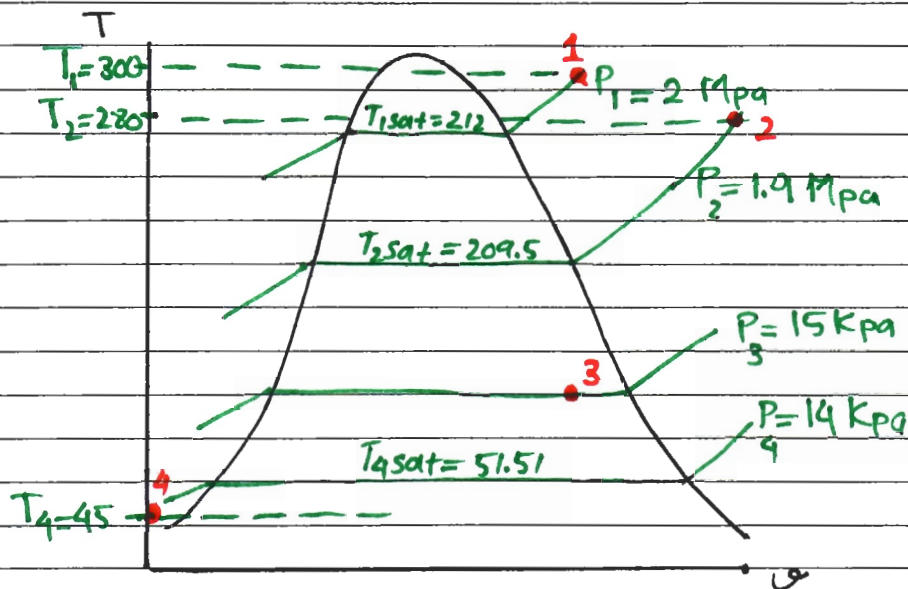


$$\left\{ \begin{array}{l} P_1 = 2 \text{ Mpa} = 20 \text{ bar} \\ T_1 = 300^\circ \text{C} \end{array} \right. \xrightarrow[\text{A}_3]{\text{Table}} T_{1\text{sat}} = 212.4^\circ \text{C}$$

$$\left\{ \begin{array}{l} P_2 = 1.9 \text{ Mpa} = 19 \text{ bar} \\ T_2 = 280^\circ \text{C} \end{array} \right. \xrightarrow[\text{A}_3]{\text{Table}} \left\{ \begin{array}{l} P_2' = 15 \text{ bar} \rightarrow T_2' = 198.3^\circ \text{C} \\ P_2'' = 20 \text{ bar} \rightarrow T_2'' = 212.4^\circ \text{C} \end{array} \right. \xrightarrow[\text{2sat}]{\text{interpolating}} T_2 = 209.5^\circ \text{C}$$

$$\left\{ \begin{array}{l} P_3 = 15 \text{ kPa} \\ x_3 = 90\% = 0.9 \end{array} \right. \rightarrow \text{Sat. Mixture}$$

$$\left\{ \begin{array}{l} P_4 = 14 \text{ kPa} \\ T_4 = 45^\circ \text{C} \end{array} \right. \xrightarrow[\text{A}_3]{\text{Table}} \left\{ \begin{array}{l} P_4' = 0.1 \text{ bar} \rightarrow T_4' = 45.81^\circ \text{C} \\ P_4'' = 0.2 \text{ bar} \rightarrow T_4'' = 60.06^\circ \text{C} \end{array} \right. \xrightarrow[\text{4sat}]{\text{interpolating}} T_4 = 51.51^\circ \text{C}$$



① & ② are Superheated vapors, ③ is mixture, ④ is subcooled (comp. liq.)

PROB.2. (Cont'd)

for ①: Superheated vapor $\xrightarrow{\text{Table A4}}$ $h_1 = \frac{2976.4 + 3069.5}{2} = \underline{\underline{3022.95}} \text{ KJ/kg}$ $T = 280^\circ\text{C}$ $T = 320^\circ\text{C}$

for ②: " " $\xrightarrow{\text{Table A4}}$ $\left\{ \begin{array}{l} h_2' = 2976.4 \\ h_2'' = 2992.2 \end{array} \right.$ $\xrightarrow[\text{Interpolation}]{\text{inter.}}$ $h_2 = \underline{\underline{2979.66}} \text{ KJ/kg}$

for ③: Mixture $\xrightarrow{\text{Table A3}}$ $h_{f3} = \frac{191.83 + 251.40}{2} = 221.61 \text{ KJ/kg}$ $P = 0.1 \text{ bar}$ $P = 0.2 \text{ bar}$

$h_{fg3} = \frac{2392.8 + 2358.3}{2} = 2374.55 \text{ KJ/kg}$

$\rightarrow h_3 = h_f + x h_{fg} = 221.61 + (0.9)(2374.55)$

$\rightarrow h_3 = \underline{\underline{2358.71}} \text{ KJ/kg}$

for ④: Subcooled $\rightarrow h_4 \approx h_f (T = 45^\circ\text{C}) \xrightarrow{\text{Table A3}}$ $h_4 = \underline{\underline{188.45}} \text{ KJ/kg}$

Mass Balance: (C.V.1)

$\dot{m}_1 = \dot{m}_2 = \dot{m}$

Energy Balance: (C.V.1)

$0 = \dot{Q}_{12} + \dot{m}_1 h_1 - \dot{m}_2 h_2 \rightarrow \dot{q}_{12} = \frac{\dot{Q}}{\dot{m}} = h_2 - h_1$

$\rightarrow \dot{q}_{12} = \underline{\underline{-43.29}} \text{ KJ/kg}$

Now for C.V.2

$\dot{m}_2 = \dot{m}_3 = \dot{m}$

$0 = -\dot{W}_T + \dot{m}_2 h_2 - \dot{m}_3 h_3 \rightarrow \dot{W}_T = \frac{\dot{W}_T}{\dot{m}} = h_2 - h_3$

$\rightarrow \dot{W}_T = \underline{\underline{620.89}} \text{ KJ/kg}$

for C.V.3

$\dot{m}_3 = \dot{m}_4 = \dot{m}$, $\dot{q}_{34} = -h_3 + h_4 = \underline{\underline{-2170.26}} \text{ KJ/kg}$

Prob. 2 (cont'd)

for C.V. 4

$$0 = 0 - \dot{w}_p + \dot{m}(h_4 - h_5) \rightarrow \dot{w}_p = \frac{\dot{w}_p}{\dot{m}} = h_4 - h_5$$

$$\rightarrow h_5 = h_4 - \dot{w}_p$$

$$= 188.45 - (4)$$

$$\rightarrow h_5 = \underline{184.45} \text{ KJ/kg}$$

for C.V. 5

$$0 = \dot{Q}_b + \dot{m}(h_5 - h_1) \rightarrow \dot{Q}_b = \frac{\dot{Q}_b}{\dot{m}} = -h_5 + h_1$$

$$\rightarrow \dot{Q}_b = -184.45 + 3022.95$$

$$\rightarrow \dot{Q}_b = \underline{2838.45} \text{ KJ/kg}$$