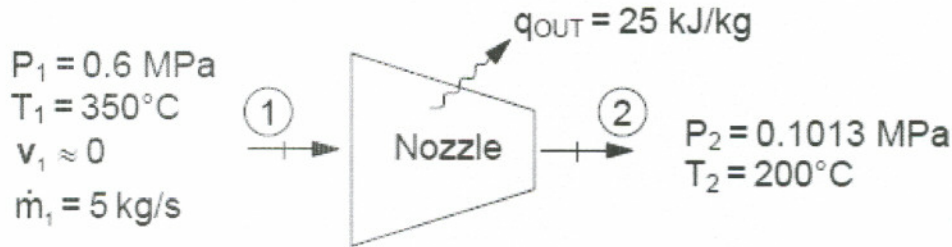


Name:

(1 Hour)

Problem 1 (10 points): A carbon dioxide nozzle is shown below. Assuming carbon dioxide is an ideal gas

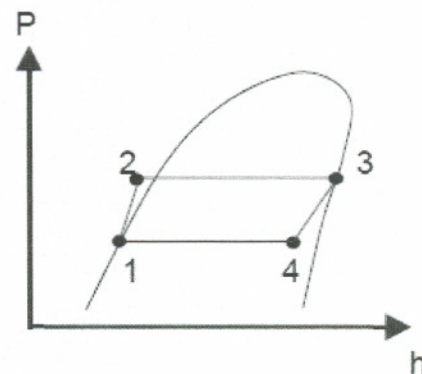
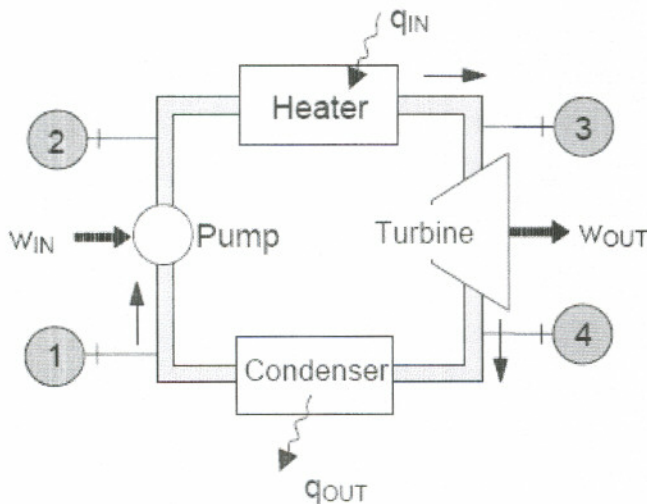
Max 19/20
Min 9/20
Avg. 12.5/20



1. Draw the P-h and T-h diagrams. (2 points)
2. Determine the exit velocity. (2 points)
3. Find the area of the nozzle at the exit. (2 points)
4. If process 1-2 is a polytropic process ($Pv^n = \text{constant}$), find power n. (2 points)
5. Add the polytropic process 1-2 to the P-h and T-h diagrams in part 1. (2 points)

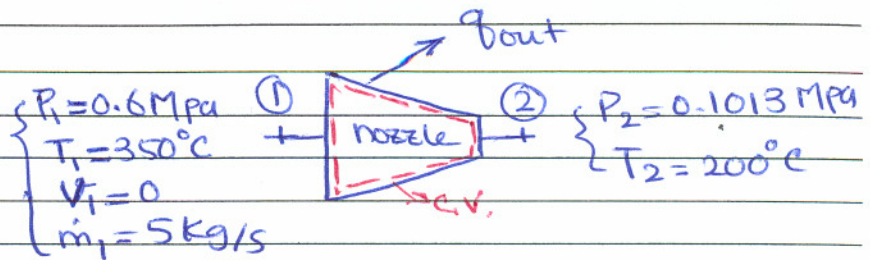
Problem 2 (10 points): A power cycle uses refrigerant R-134A as the working fluid. It operates between pressures of 60 and 600 kPa, and the states at the process endpoints are shown on the P-h diagram. The quality (x) at state 4 is 0.98.

1. Construct a state table for this heat engine. (7 points)
2. Find $w_{\text{NET}}/q_{\text{IN}}$, explain what is this quantity. (3 points)



PROBLEM 1

CO₂
ideal gas



Mass Balance:

$$\frac{d\dot{m}_{cv}}{dt} = \sum \dot{m}_i - \sum \dot{m}_o \Rightarrow 0 = \dot{m}_1 - \dot{m}_2 \Rightarrow \dot{m}_1 = \dot{m}_2 = 5 \text{ kg/s}$$

o (s.s.)

Energy Balance:

$$\frac{dE_{cv}}{dt} = \sum \dot{Q} - \sum \dot{W} + \sum \dot{m}_i \left(h_i + \frac{V_i^2}{2} + gz_i \right) - \sum \dot{m}_e \left(h_e + \frac{V_e^2}{2} + gz_e \right)$$

o (s.s.)

$$0 = q + h_1 - h_2 - \frac{V_2^2}{2} \rightarrow V_2 = \sqrt{2(q + h_1 - h_2)}$$

Table A23

T = 620 K $\bar{h} = 23231 \text{ kJ/kmol}$

T = 630 K $\bar{h} = 23709 \text{ kJ/kmol}$

$T_1 = 350 + 273 = 623 \text{ K} \xrightarrow{\text{interpolate}} \bar{h}_1 = 23386 \text{ kJ/kmol} = \frac{23386}{44} = 531.50 \text{ kJ/kg}$

$M_{\text{CO}_2} \swarrow$

Table A23

T = 470 K $\bar{h} = 16351 \text{ kJ/kmol}$

T = 480 K $\bar{h} = 16791 \text{ kJ/kmol}$

$T_2 = 473 \text{ K} \rightarrow \bar{h}_2 = 16492.1 \frac{\text{kJ}}{\text{kmol}} = 374.82 \frac{\text{kJ}}{\text{kg}}$

the relation with temperature for an ideal gas

$$\left(\frac{P_1}{P_2}\right)^{\frac{n-1}{n}} = \frac{T_1}{T_2} \xrightarrow{\text{take}} \ln \left(\frac{P_1}{P_2}\right)^{\frac{n-1}{n}} = \ln\left(\frac{T_1}{T_2}\right)$$

$$\rightarrow \left(\frac{n-1}{n}\right) \left(\ln\left(\frac{0.6}{0.1013}\right)\right) = \ln\left(\frac{350+273}{200+273}\right)$$

$$\rightarrow n = 1.1832 \text{ Ans.}$$

To add the polytropic process to the P-h and T-h diagrams we need to find another value of h in each case.

if assuming $c_p = \text{constant}$ (is valid for graphing purposes)

the $h = c_p T \rightarrow \left(\frac{P_1}{P_2}\right)^{\frac{n-1}{n}} = \frac{h_1/c_p}{h_2/c_p} = \frac{h_1}{h_2}$

$$\rightarrow \frac{h_1}{h_2} = \left(\frac{P_1}{P_2}\right)^{0.154} \rightarrow \text{at an arbitrary point with } P_3 = 0.4 \text{ MPa for example}$$

$$\rightarrow \frac{h_1}{h_3} = \left(\frac{P_1}{P_3}\right)^{0.154} \rightarrow \frac{531.50}{h_3} = \left(\frac{0.6}{0.4}\right)^{0.154}$$

$$\rightarrow h_3 = 499.15 \text{ kJ/kg}$$

$$\text{and } \frac{T_1}{T_3} = \left(\frac{P_1}{P_3}\right)^{0.154} \Rightarrow \frac{T_1}{h_3} \rightarrow T_3 = 585.09 \text{ K} \\ = 312^\circ \text{C}$$

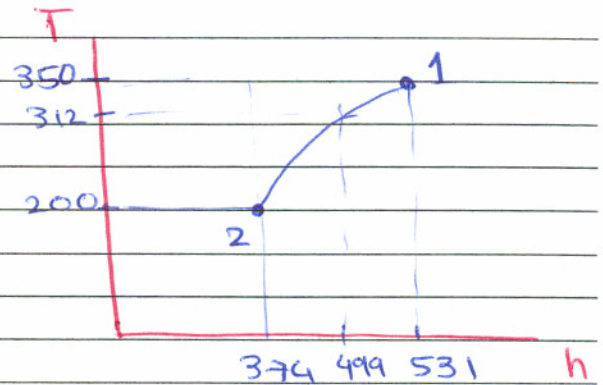
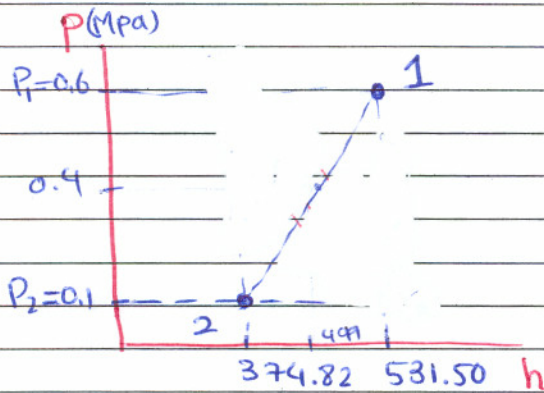
Prob 1 (cont'd)

plugging for h_1 and h_2

$$V_2 = \sqrt{2(25 + 531.50 - 374.82) \times 1000}$$

Kilo \rightarrow

$$\rightarrow V_2 = 513.2 \text{ m/s Ans.}$$



$$\dot{m} = \rho AV \rightarrow \dot{m}_2 = \rho_2 A_2 V_2 \rightarrow \dot{m}_2 = \frac{A_2 V_2}{v_2} \quad (1)$$

CO₂ ideal gas \rightarrow Table A20, $T = 200^\circ\text{C} \rightarrow R_{\text{CO}_2} = ?$

$$T = 400 \rightarrow R_{\text{CO}_2} = C_p - C_v = 0.189 \text{ kJ/kgK}$$

and R stays almost constant.

for an ideal gas we have $Pv = RT$

$$\rightarrow v_2 = \frac{R_{\text{CO}_2} T_2}{P_2} = \frac{0.189 \times (200 + 273)}{101.3 \text{ kPa}} = 0.8825 \frac{\text{m}^3}{\text{kg}}$$

now plugging into (1) $A_2 = \dot{m}_2 v_2 / V_2$

$$\rightarrow A_2 = 5 \times 0.8825 / 513.2 = 85.98 \text{ cm}^2 \text{ Ans.}$$

Polytropic then $Pv^n = \text{const} \rightarrow P_1 v_1^n = P_2 v_2^n$ or use

Problem 2

$$P_1 = P_4 = 60 \text{ kPa}$$

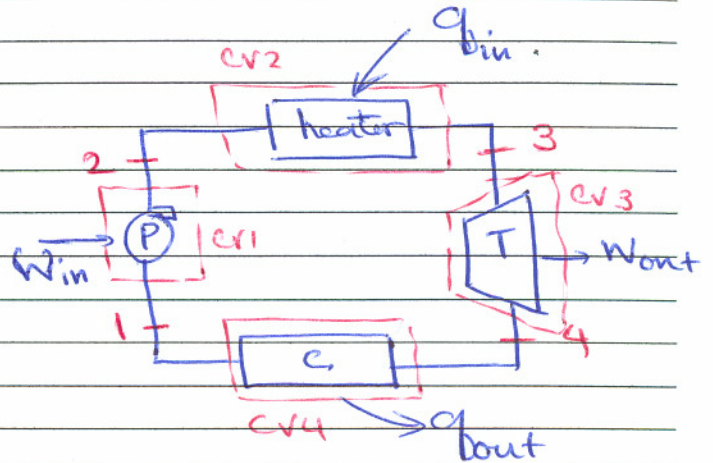
$$P_2 = P_3 = 600 \text{ kPa}$$

$$x_4 = 0.98$$

$$x_1 = 0$$

$$x_3 = 1$$

R-134A, steady state



C.V. 1

$$\text{mass balance: } \dot{m}_1 = \dot{m}_2$$

$$\text{energy balance: } 0 = -\dot{W}_{in} + \dot{m}(h_2 - h_1)$$

$$\text{or } \dot{W}_{in} = \dot{m}(h_2 - h_1)$$

C.V. 2

$$\text{M.B.: } \dot{m}_2 = \dot{m}_3$$

$$\text{E.B.: } 0 = \dot{q}_{in} + \dot{m}(h_2 - h_3)$$

C.V. 3

$$\text{MB: } \dot{m}_3 = \dot{m}_4$$

$$\text{E.B.: } 0 = -\dot{W}_{out} + (\dot{m})(h_3 - h_4)$$

$$\text{or } \dot{W}_{out} = \dot{m}(h_3 - h_4)$$

C.V. 4

$$\text{MB: } \dot{m}_4 = \dot{m}_1$$

$$\text{E.B.: } 0 = \dot{q}_{out} + \dot{m}(h_4 - h_1)$$

Finding the properties

point 1: saturated liquid $x=0$ Table A11 $\rightarrow h_1 = h_f = 3.46$ KJ/kg
 $P = 60 \text{ kPa} = 0.6 \text{ bar}$
 $v_1 = v_f = 7097 \times 10^{-3}$

Point 3: Saturated vapor $x=1$ Table A11 $\rightarrow h_3 = h_g = 259.19$
 $P = 600 \text{ kPa} = 6 \text{ bar}$
 $v_3 = v_g = 0.0341$

Point 4: mixture $x=0.98$, $P = 60 \text{ kPa} = 0.6 \text{ bar}$

Table $\rightarrow h_f = 3.46$, $h_g = 224.72 \rightarrow h = (1-x)h_f + xh_g$

$$\rightarrow h_4 = (1-0.98)(3.46) + 0.98(224.72)$$

$$\rightarrow h_4 = 220.295 \text{ KJ/kg}$$

for the pump we have (C.V. 1)

$$\dot{W}_{in} = (h_1 - h_2)$$

to find h_2 we also know work done by a pump is

$$W_p = -\dot{W}_{in} = \int v \, dp = v_1 (P_2 - P_1)$$

then

$$-(h_1 - h_2) = v_1 (P_2 - P_1) \rightarrow h_2 = h_1 + v_1 (P_2 - P_1)$$

$$= 3.46 + 0.7097 \times 10^{-3} \times (600 - 60)$$

$$h_2 = 3.84 \text{ KJ/kg}$$

$$\text{then } W_{in} = h_1 - h_2 = -0.38 \text{ KJ/kg}$$

$$q_{in} = h_3 - h_2 = 255.35 \text{ KJ/kg}$$

$$W_{out} = h_3 - h_4 = 38.89 \text{ kJ/kg}$$

$$q_{out} = h_1 - h_4 = -216.84 \text{ kJ/kg}$$

$$\text{then } \frac{W_{net}}{q_{in}} = \frac{W_{out} - W_{in}}{q_{in}} = \frac{38.89 - 0.38}{255.35} = \frac{-0.1508}{-0.1508} = 15.1\%$$

this the efficiency of the cycle,