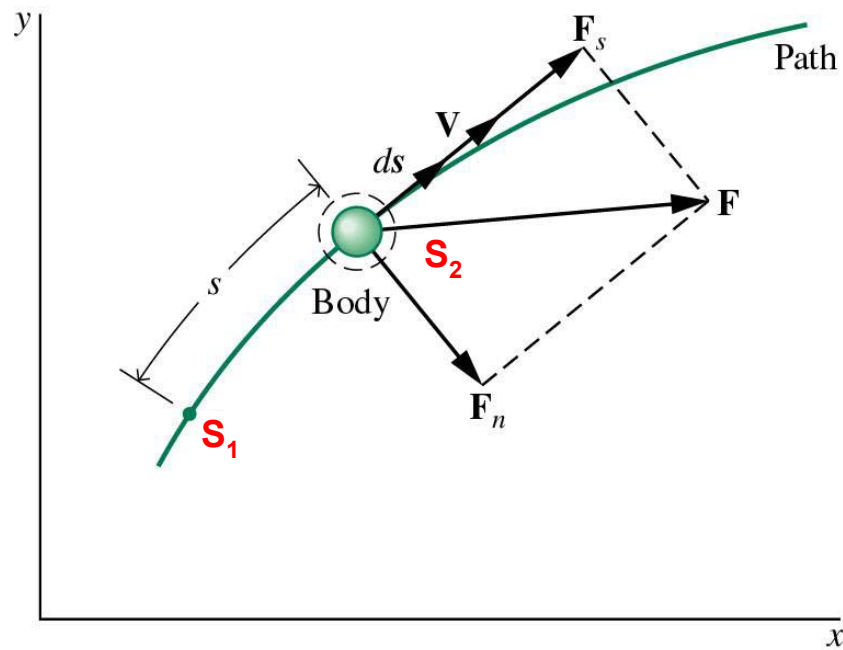


We will cover the following concepts,

- ***Work, Kinetic and Potential Energy***
- ***Conservation of Energy***
- ***Power***
- ***Work Sign Convention***
- ***Expansion or Compression Work***

A body moves from point  $s_1$  with velocity  $V_1$  to point  $s_2$  with velocity  $V_2$ .



Newton's 2<sup>nd</sup> law:  $F = m \cdot a$  then

$$F_s = m \frac{dV}{dt}$$

$$= m \frac{dV}{ds} \frac{ds}{dt} = m \frac{dV}{ds} V$$

Integrated from  $s_1$  point  $s_2$

$$\int_{V_1}^{V_2} mVdV = \int_{s_1}^{s_2} F_s ds$$

Evaluating

$$\underbrace{\frac{1}{2}m(V_2^2 - V_1^2)}_{\text{Kinetic Energy}} = \underbrace{\int_{s_1}^{s_2} F_s ds}_{\text{Work}}$$

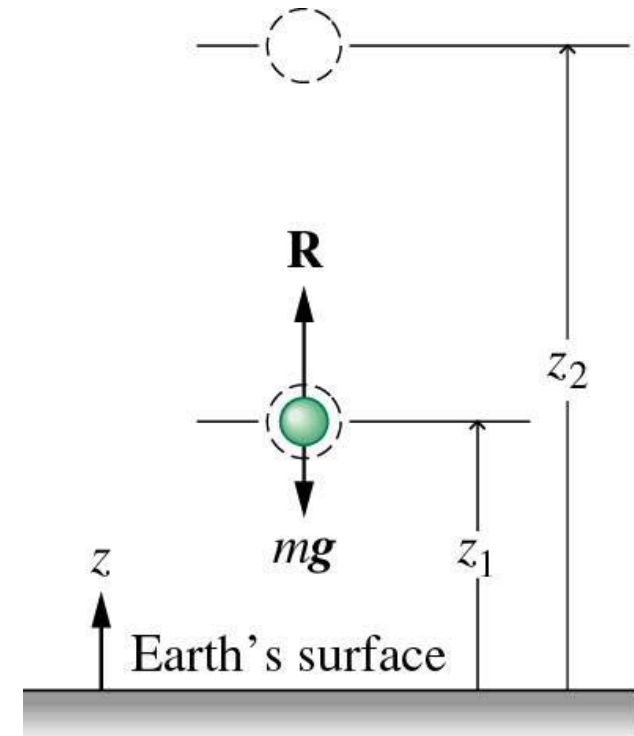
$$\Delta KE = KE_2 - KE_1 = \Delta W$$

A body moves from point  $z_1$  with velocity  $V_1$  to point  $z_2$  with velocity  $V_2$ .

**Energy Balance:**

$$\frac{1}{2}mV_2^2 + mgz_2 = \frac{1}{2}mV_1^2 + mgz_1 + \int_{z_1}^{z_2} R dz$$

$$\Delta PE = PE_2 - PE_1 = mg(z_2 - z_1)$$



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**The rate of energy transfer by work is called power.**

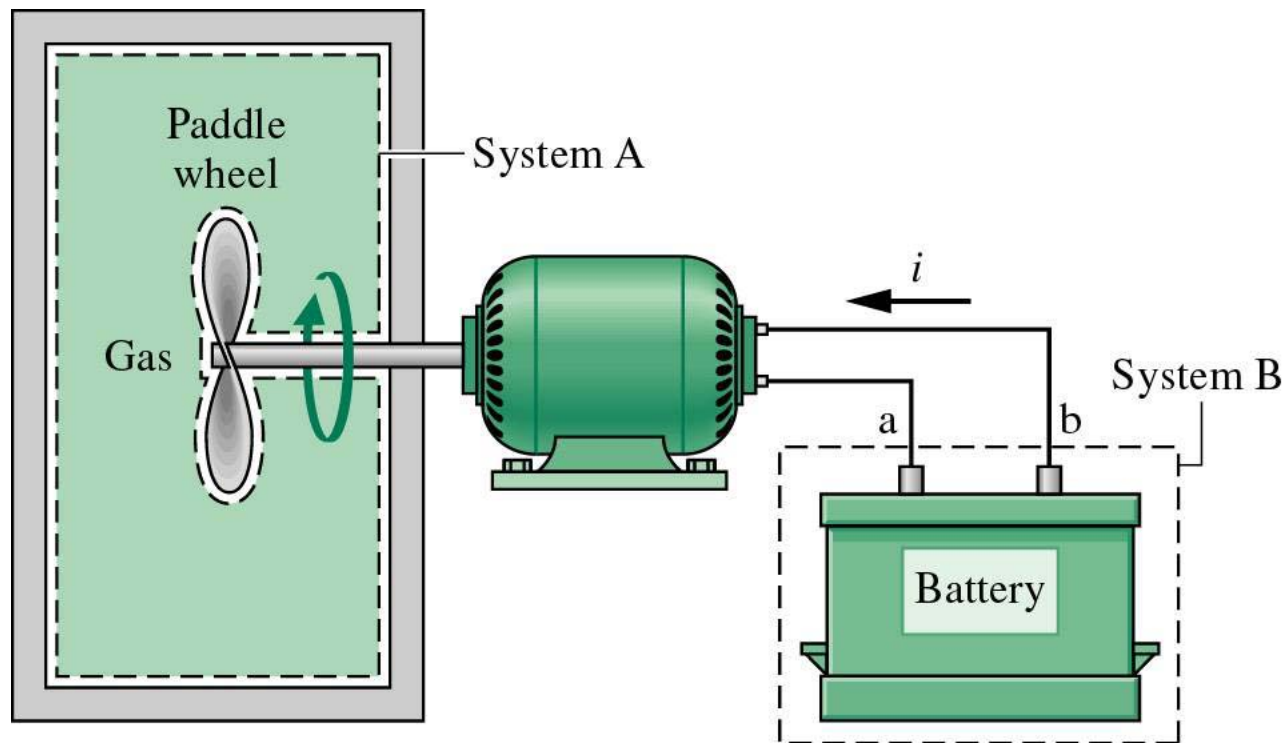
$$\dot{W} = \frac{\text{Work}}{\text{Time}} = \frac{dW}{dt} = F.V$$

$$W = \int_{t_1}^{t_2} \dot{W} dt = \int_{t_1}^{t_2} F.V dt = \int_{s_1}^{s_2} F. \frac{ds}{dt} dt$$

$$W = \int_{s_1}^{s_2} F.ds$$

$W > 0$ : work done *by* the system

$W < 0$ : work done *on* the system



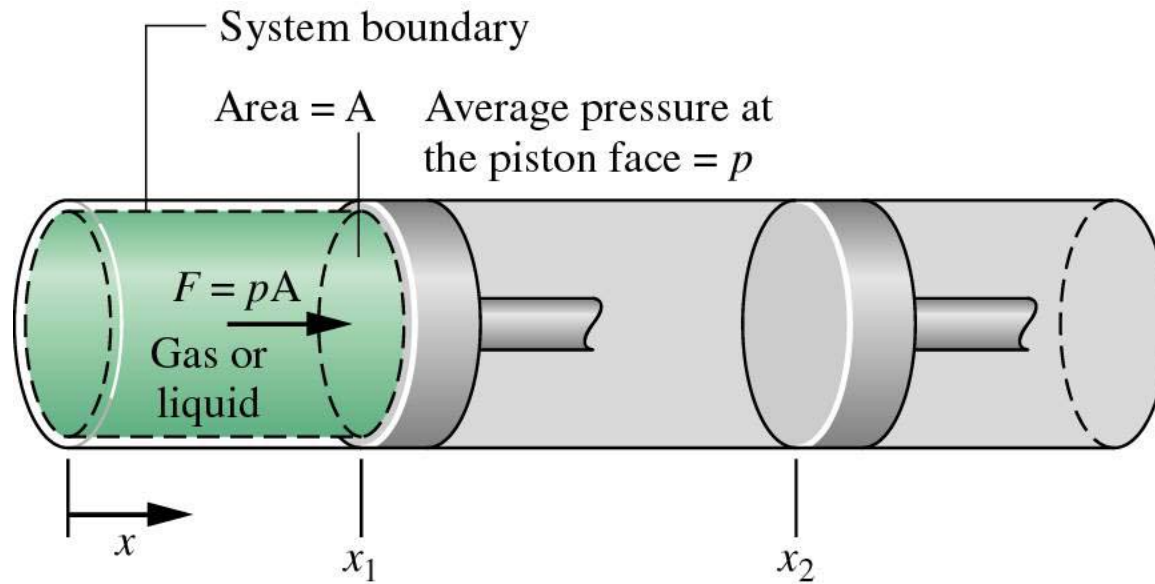
Work is not a property of the system or the surroundings so we can not say the amount of work at state 1 is  $W_1$ . It can only be defined for a process, meaning the work done on/by the system from state 1 to state 2.

$$W = \int_1^2 \delta W$$

$\delta W$  is called inexact.

How about this integral? Is velocity exact or inexact?

$$\int_{V_1}^{V_2} dV = V_2 - V_1$$



$$\begin{aligned}\delta W &= pA dx \\ &= p dV\end{aligned}$$

$$W = \int_{V_1}^{V_2} p dV$$