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Erik Bollt^{a)}

AFFILIATIONS

Department of Electrical and Computer Engineering, Clarkson University, Potsdam, New York 13699, USA and Clarkson Center for Complex Systems Science (C^3S^2), Potsdam, New York 13699, USA

^{a)}Author to whom correspondence should be addressed: bolltem@clarkson.edu

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In our recent paper, with $\mathbf{w} = [w_1 | w_2 | \cdots | w_n]^T$ and $\mathbf{b} = [b_1 | b_2 | \cdots | b_n]$, we correct the following typographical error, which is important for correctly implementing the NVAR, discussed in Sec. VI and Appendix B. A typo occurred in Eq. (B3), which was a result of a problem of indexing the appearance of $\mathbf{b}_2 \circ \mathbf{b}_2$ in the second line of Eq. (B3), which should rather be $\mathbf{b}_1 \circ \mathbf{b}_2$. So, the correct equation is

$$B\mathbf{w} \circ B\mathbf{w} = (w_1\mathbf{b}_1 + w_2\mathbf{b}_2 + \dots + w_n\mathbf{b}_n) \circ (w_1\mathbf{b}_1 + w_2\mathbf{b}_2 + \dots + w_n\mathbf{b}_n)$$

$$= [\mathbf{b}_{1} \circ \mathbf{b}_{1} | \mathbf{b}_{1} \circ \mathbf{b}_{2} | \cdots | \mathbf{b}_{n} \circ \mathbf{b}_{n}] \begin{bmatrix} w_{1}^{2} \\ w_{1}w_{2} \\ \vdots \\ w_{1}w_{n} \\ w_{2}w_{1} \\ w_{2}^{2} \\ \vdots \\ w_{n}^{2} \end{bmatrix} := P_{2}(B, B) p_{2}(\mathbf{w}, \mathbf{w}). \tag{1}$$

However, for the sake of clarity and to lay more emphasis on detail, we may write the term in the second line as

$$[\mathbf{b}_1 \circ \mathbf{b}_1 | \mathbf{b}_1 \circ \mathbf{b}_2 | \cdots | \mathbf{b}_n \circ \mathbf{b}_n] = [\mathbf{b}_1 \circ \mathbf{b}_1 | \mathbf{b}_1 \circ \mathbf{b}_2 | \cdots | \mathbf{b}_1 \circ \mathbf{b}_n | \mathbf{b}_2 \circ \mathbf{b}_1 | \mathbf{b}_2 \circ \mathbf{b}_2 | \cdots | \mathbf{b}_{n-1} \circ \mathbf{b}_n | \mathbf{b}_n \circ \mathbf{b}_n]. \tag{2}$$

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¹E. Bollt, "On explaining the surprising success of reservoir computing forecaster of chaos? The universal machine learning dynamical system with contrast to VAR and DMD," Chaos 31(1), 013108 (2021).